

جدول مشتق تابع

رديف	تابع	مشتق تابع	نمونه
1	$y = k$	$y' = k$	$y = v \rightarrow y' = 0$ $y = -\frac{v}{x} \rightarrow y' = \frac{1}{x}$
2	$y = kx$	$y' = k$	$y = vx \rightarrow y = v$ $y = x \rightarrow y' = 1$ $y = -x \rightarrow y' = -1$
3	$y = x^n$	$y' = nx^{n-1}$	$y = x^{\delta} \rightarrow y' = \delta x^{\gamma}$
4	$y = ku$	$y' = ku'$	$y = vx^{\gamma} \rightarrow y' = \gamma vx^{\gamma-1}$
5	$y = u \pm v$	$y' = u' \pm v'$	$y = vx^{\gamma} - \delta x^{\gamma} + x - 1$ $\rightarrow y' = \gamma vx^{\gamma-1} - \gamma \cdot x + 1$
6	$y = u^n$	$y' = nu'u^{n-1}$	$y = (x^{\gamma} - x + 1)$ $\rightarrow y' = 1 \cdot (\gamma x - 1)(x^{\gamma-1} - x + 1)$
7	$y = uv$	$y' = u'v + v'u$	$y = (\gamma x + 1)(x^{\gamma} + x)$ $\rightarrow y' = \gamma(x^{\gamma-1} + x) + (\gamma x + 1)(\gamma x + 1)$
8	$y = \frac{u}{v}$	$y' = \frac{u'v - v'u}{v^2}$	$y = \frac{vx - 1}{x^{\gamma} + x} \rightarrow$ $y' = \frac{\gamma(x^{\gamma-1} + x) - (\gamma x + 1)(\gamma x - 1)}{(x^{\gamma} + x)^2}$
9	$y = \frac{ax + b}{cx + d}$	$y' = \frac{ad - bc}{(cx + d)^2}$	$y = \frac{vx - 1}{\gamma x + \gamma} \rightarrow$ $y' = \frac{\gamma x - (-\gamma)}{(\gamma x + \gamma)^2} = \frac{\gamma}{(\gamma x + \gamma)^2}$
10	$y = \sqrt{u}$	$y' = \frac{u'}{2\sqrt{u}}$	$y = \sqrt{x} \rightarrow y' = \frac{1}{2\sqrt{x}}$ $y = \sqrt{vx + 1} \rightarrow y' = \frac{v}{2\sqrt{vx + 1}}$

11	$y = \sqrt[n]{u^m}$	$y' = \frac{mu'}{n\sqrt[n]{u^{n-m}}}$	$y = \sqrt[r]{1+x^r} \rightarrow y' = \frac{r(1+x^r)^{\frac{r-1}{r}}}{r\sqrt[r]{(1+x^r)}^r}$
12	$y = u $	$y' = \frac{u'u}{ u }$	$y = x \rightarrow y' = \frac{x}{ x }$ $y = x^r - 1 \rightarrow y' = \frac{rx(x^r - 1)}{ x^r - 1 }$
13	$y = \sin u$	$y' = u' \cos u$	$y = \sin x \rightarrow y' = \cos x$ $y = \sin(x^r - x) \rightarrow y' = (rx^r - 1)\cos(x^r - x)$
14	$y = \cos u$	$y' = -u' \sin u$	$y = \cos x \rightarrow y' = -\sin x$ $y = \cos \sqrt{x} \rightarrow y' = \frac{-1}{\sqrt{x}} \sin \sqrt{x}$
15	$y = \tan u$	$y' = u'(1 + \tan^r u)$	$y = \tan x \rightarrow y' = (1 + \tan^r x)$ $y = \tan(x^r + 1) \rightarrow y' = rx^r(1 + \tan^r(x^r + 1))$
16	$y = \cot u$	$y' = -u'(-1 + \cot^r u)$	$y = \cot x \rightarrow y' = -(1 + \cot^r x)$ $y = \cot(rx + 1) \rightarrow y' = -r(1 + \cot^r(rx + 1))$
17	$y = e^u$	$y' = u'e^u$	$y = e^x \rightarrow y' = e^x$ $y = e^{\sin x} \rightarrow y' = \cos x e^{\sin x}$
18	$y = \ln u$	$y' = \frac{u'}{u}$	$y = \ln x \rightarrow y' = \frac{1}{x}$ $y = \ln(rx^r - x + 1) \rightarrow y' = \frac{rx^r - 1}{rx^r - x + 1}$
19	$y = a^u \left(\begin{array}{l} a > 0 \\ a \neq 1 \end{array} \right)$	$y' = u'(\ln a)a^u$	$y = \delta^{\sqrt{x}} \rightarrow y' = \frac{1}{\sqrt{x}} \ln \delta(\delta^{\sqrt{x}})$
20	$y = u^v$	$y' = \left(v' \ln u + \frac{u'}{u} v \right) u^v$	$y = (x^r - x)^{vx+1} \rightarrow$ $y' = \left(v \ln(x^r - x) + \frac{rx^r - 1}{x^r - x} (vx + 1) \right) (x^r - x)^{vx+1}$

21	$y = \log_a^u$	$y' = \frac{u'}{u \ln a}$	$y = \log_{\Delta}^{(x^r - x)} \rightarrow y' = \frac{rx - 1}{(x^r - x) \ln \Delta}$
22	$y = \sin^{-1} u$	$y' = \frac{u'}{\sqrt{1-u^2}}$	$y = \sin^{-1}(\Delta x^r - 1) \rightarrow y' = \frac{1 \cdot x}{\sqrt{1-(\Delta x^r - 1)^2}}$
23	$y = \cos^{-1} u$	$y' = \frac{-u'}{\sqrt{1-u^2}}$	$y = \cos^{-1}(rx - 1) \rightarrow y' = \frac{-(r)}{\sqrt{1-(rx - 1)^2}}$
24	$y = \tan^{-1} u$	$y' = \frac{u'}{1+u^2}$	$y = \tan^{-1} \sqrt{x} \rightarrow y' = \frac{1}{\sqrt{1+\left(\sqrt{x}\right)^2}}$
25	$y = \cot^{-1} u$	$y' = \frac{-u'}{1+u^2}$	$y = \cot^{-1} x \rightarrow y' = \frac{-1}{1+x^2}$